

Capital Asset Pricing Model

I. CAPM: Assumptions and Prediction

1. Perfect markets
 - Perfect competition: Each investor has no effect on prices or returns
 - No taxes
 - No transaction costs
 - All assets are traded and perfectly divisible
 - No short sale constraints
 - Borrow and lend at the same risk-free rate, total borrowing = total lending
2. Investors only worry about mean and variance of end-of-period wealth
3. Homogeneous expectations

Under these assumptions, CAPM says that the return of any Stock i , r_i , should satisfy

$$E[r_i] = r_f + \beta_i [E(r_M) - r_f]$$

Where r_f is the risk free rate, r_M is the market portfolio return, and

$$\beta_i = \frac{\text{Cov}(r_i, r_M)}{\text{Var}(r_M)}$$

II. CAPM Market Portfolio and Risk-Free Rate

- A. How do we know that everyone would invest only in same portfolio?

- B. How do we know that the market will be “cleared”—that everyone gets to invest however much they want in the efficient portfolio?

Notice that if some investors become less risk-averse, the market portfolio becomes more risky.

Note: Under the assumption of CAPM, the market portfolio should include all wealth. However, we typically use a portfolio of exchange-traded stocks. For example, we might use the value-weighted index of NYSE stocks

III. Beta Pricing

- A. Where does the beta pricing formula come from?

B. What does the CAPM Beta formula says?

1. β measures each asset's contribution to the variance of the market portfolio, which we know is the optimal portfolio. (You will be asked to derive this property of β in Assignment 1.)
2. Investors only care about the risk and expected return of their *optimal portfolios*. Therefore, they are only concerned with the impact of an additional asset on the risk and return of their portfolio.
3. Since the only relevant risk of an asset is its *marginal contribution to the risk of the market portfolio*, this is the only risk that gets compensated.

For an asset that goes against the market, its return should be negative!
Why?